Application: AEF-A.7 Assembly on square profile

KEY WORDS

Non-linear static analysis, Spatial state of stresses, Linear material, 3D geometric model, 3D finite element, Non-linear finite element (parabolic), Cylindrical coordinate system, Mechanical contact with friction, Structural error, Assembly on square profile, Mechanical subassembly

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A. PROBLEM DESCRIPTION

A.1. Introduction

FEA, as a general method of studying physical phenomena and processes in mechanical structures also allows the analysis of the mechanical fields that appear in the case of *the contacts of the mechanical assemblies* that suppose the elastic deformable surfaces from the direct contacts and of the slip friction that occur between them.

The profiled (polygonal) assemblies with the advantages of the increased load-carrying capacity and the good centering have disadvantages related to the very complex stress state in the contact areas, which requires modeling and FEA for design.

A.2. Application description

For the design of the crank of the mechanism that transforms the movement of swing of translation into movement of swing of rotation (fig. a) the head area of the driven shaft will be considered. The profiled (polygonal) square assembly of the figure *transmits the forces* from crank 1 to the square shaft 2 *by shape* (fig. b). For the design of the crank based on FEA, it is necessary to consider the interactions of its four internal contact surfaces with the four contact surfaces machined on the shaft. Although, the transmission of the forces from the crank to the shaft is done by form, in the four contacts during the elastic deformation of the materials in contact there appear relative litle spliping movements and therefore also frictional forces.



For this application, FEA is required for the displacement and stress fields in crank 1, including the shaft assembly with shaft 2. The crank is made of E335 soft steel and the improved C45 hard steel shaft. The dimensions of the assembly elements are: L = 100, h = 10 mm, H = 30 mm, a = 45 mm, b = 50 mm, R = 16 mm, r = 8 mm. The crank is loaded with tangential force F = 10000 N and axial $F_a = 2000$ N.

B. THE FEA MODEL

B.1. The model definition

In order to design the crank FEA model, it is necessary to consider and a portion of the driven shaft adopting the following simplifying hypotheses:

- considering friction in mechanical contacts,
- adoption of material strength constraints (embedding, concentrated force action),
- the material has elastic linear behavior,
- the deformation occurs static (the variation of the deformation force with time is not taken into account).

B.2. The analysis model description

The model for analysis is based on the 3D geometric model of the crank (fig. a) in contact with friction with the 3D model of the shaft (fig. b). For analysis the structure is composed of two solids (crank and shaft) which are generated by extrusion and discretized with 3D finite elements.

In order to make the *mechanical contacts between the crank and the shaft* on flat surfaces, the square profile of the crank will be connected to the corners with 2.5 mm radius and the shaft one will be 2.5 mm (fig. A, b). In order to simulate the behavior of the assembly as close to reality when modeling the mechanical contacts between elastic deformable surfaces, the friction coefficient $\mu = 0.2$ will be considered.

The loading of the model for the analysis will be carried out in the area of the crankshaft coupling (subchapter A.2, fig. a) with the tangential forces, 20000 N, and axial 4000 N (fig. a, b). The modeling of the loads with these forces will be done with the specific function "Bearing Load".



For the analysis with finite elements the strength characteristics of the materials are:

- longitudinal modulus of elasticity $E = 205000 \text{ N} / \text{mm}^2$ (MPa), coefficient of transverse contraction (Poisson) v = 0.29, for steel E335 ($\sigma_{02} = 335\text{MPa} \text{at}$ traction; $\sigma_{02} = 400 \text{ MPa} \text{at}$ compression; $\sigma_r = 590...760 \text{ MPa}$) associated with Manivelă element.
- the longitudinal elasticity modulus E = 210000 N / mm2, the coefficient of transverse contraction (Poisson) v = 0.3, for the C45 alloy carbon steel (0.4% C) associated with the Arbore solid which, after the hardening treatment, reaches at hardness 250 ... 280 HB ($\sigma_{02} = 520 \text{MPa} \text{at traction}; \sigma_{02} = 560 \text{ MPa} \text{at compression}; \sigma_r = 690...860 \text{ MPa}$)

The average working temperature of the subassembly, $T_0 = 22^0$ C.

C. PREPROCESSING OF FEA MODEL

C.1 Activarea și salvarea proiectului / Creating, setting and saving the project
Creating of the project
Λ , Toolbox : \Box Analysis Systems $\rightarrow \Box \Box$ Static Structural (the subproject window appears automatically); \rightarrow
[the name can be changed Static Structural in Assem_sq].
<u>Problem type setting (2D)</u>
A: L 🥯 Geometry - Properties - Properties of Schematic A3: Geometry , E Advanced Geometry Options : Analysis Type ,
[select from list with \square , \square] (this setting is usually default) \rightarrow [close the window \square].
Save of the project
\downarrow Save As \rightarrow \bigwedge Save As, File name: [input name, AEF-A.7] $\rightarrow \downarrow$ Save

C.2 Modelling of material and environment characteristics
Generating of the material characteristics for the component Manivelă
N, Project Schematic: L, $<$ Engineering Data $<$ _ \rightarrow $<$ Edit \rightarrow Outline of Schematic A2: Engineering Data $<$ $<$
Click here to add a new material \rightarrow [input name: E335] (it appear in line $2^{\text{E335}} \rightarrow 12^{\text{E335}} \rightarrow 10^{\text{Toolbox}}$:
🗄 Linear Elastic 🛶 🗐 Isotropic Elasticity 🛶 Table of Properties Row 2: Isotropic Elasticity Temperature (C) 💺 🔶 select
from list with $\downarrow \stackrel{\checkmark}{=} C$ (grade Celsius) input value, 20], Young's Modulus (Pa) $\checkmark \rightarrow$ [select from list with $\downarrow \stackrel{\checkmark}{=}$

MPa, input value 205000], Poisson's Ratio \rightarrow [input value 0,29] (the window is automatically generated Properties of Outline Row 4: E335] and the graph Chart of Properties Row 2: Isotropic Elasticity, in which the data entered are
Generating of limit and permissible characteristics of the material E335
Λ , Toolbox: I Strength \rightarrow 2 Tensile Yield Strength \rightarrow Properties of Outline Row 4: E335: 2^{12} Tensile Yield Strength, [select
from list with \rightarrow MPa input value, 335] (traction limit stress). Toolbox: \rightarrow Strength \rightarrow Compressive Yield Strength \rightarrow Properties of Outline Row 4: E335: 2 Compressive Yield Strength,
[select from list with \downarrow MPa, input value, 400] (compression limit stress). Toolbox: \downarrow Strength \rightarrow Tensile Ultimate Strength \rightarrow Properties of Outline Row 4: E335: 2 ^C Tensile Ultimate Strength
$ [select from list with \downarrow \blacksquare MPa / input value, 220] (traction admisible stress). \\ \hline Toolbox: \downarrow \blacksquare Strength \rightarrow \textcircled{Compressive Ultimate Strength} \rightarrow \r{l} Properties of Outline Row 4: E335 : $
² Compressive Ultimate Strength, [select from list with stress).
Generating of the material characteristics for the component Arbore
Λ , Project Schematic : L, \ll Engineering Data \checkmark \rightarrow \rightarrow \ll Edit \rightarrow Outline of Schematic A2: Engineering Data \sim \downarrow
Click here to add a new material \rightarrow [input name C45] (it apear in line 4 ? $^{\circ}$ C45) $\rightarrow \downarrow$? $^{\circ}$ C45 \rightarrow Toolbox:
🗄 Linear Elastic 🛶 🖓 Isotropic Elasticity 🛶 Table of Properties Row 2: Isotropic Elasticity : Temperature (C) 📮 🔶 [select
from list with $\downarrow \stackrel{>}{\longrightarrow} C$ (grade Celsius) input value, 20], Young's Modulus (Pa) $\checkmark \rightarrow$ [select from list with $\downarrow \stackrel{>}{\longrightarrow}$ MPa / input value, 210000], Poisson's Ratio \rightarrow [input value 0,3] (the window is automatically generated Properties of Outline Row 4: E335 and the graph Chart of Properties Row 2: Isotropic Elasticity, in which the data entered are highlighted)
Generating of limit and permissible characteristics of the material C45
\wedge Toolbox \square Extended \square Tensile Yield Strength \square Properties of Outline Row 5: C45 \square Tensile Yield Strength [select
from list with JIMPa / input value, 520] (/ traction limit stress).
Toolbox 🔄 🗄 Strength 🛶 🔀 Compressive Yield Strength 🛶 Properties of Outline Row 5: C45 💡 🔀 Compressive Yield Strength
[select from list with I MPa / input value, 560] (compression limit stress).
Toolbox : 🗇 🗄 Strength 🕁 🎦 Tensile Ultimate Strength 🛶 Properties of Outline Row 5: C45 : ? 🎦 Tensile Ultimate Strength , [select
from list with \rightarrow MPa / input value, 420] (traction admisible stress). Toolbox: \rightarrow Strength \rightarrow Compressive Ultimate Strength \rightarrow Properties of Outline Row 5: C45 : ? Compressive Ultimate Strength
, [select from list with I MPa / input value, 480] (compresion limit stress).
Update of the database and exit
Λ \downarrow \checkmark Update Project \rightarrow \downarrow \bigcirc Return to Project
C.3. Geometric modelling
C.3.1 Model loading, DesignModeler (DM)
Λ , Project Schematic: \Box Geometry $\rightarrow \Box$ Wew Geometry \rightarrow ANSYS Workbench: \Box Millimeter, \Box OK.

C.3.2 Sketch 1 generation (Shaft)

Viewing default plane (XY)

(Look at face/Plane/Schetch) \rightarrow (automatically view of default plane XY Plane);

Generating of rectangular contour

Sketching Toolboxes: \Box Draw $\rightarrow \Box$ Rectangle \rightarrow [a rectangular line is generated in the center area of the XY plane, marking with \dashv the first (quadrant II) corner and the release \dashv in the opposite corner (quadrant IV)] (fig. a).

Centering of rectangular contour

Sketching Toolboxes: \Box **Constraints** $\rightarrow \Box$ **if** Symmetry \rightarrow [select with \Box the Y axis followed by the select selection of the two lines parallel to the Y axis (the two sides will be positioned centered relative to the Y axis)] (fig. b) \rightarrow [is selected with \Box a dot in the model area] $\rightarrow \Box$ **Select new symmetry axis** \rightarrow [select with \Box the X axis followed by the selection with \Box of the two lines parallel to X (the two sides will be centered centered with X)] (fig. b).





<i>a. b.</i>
C.3.6 Generating the surface and body of the crank hub
$\underbrace{Generating the surface for the hub}{\mathbb{G}}$
Details of SurfaceSk : \Box Base Objects $\rightarrow \Box$ Apply; \Box \neq Generate (surface generating, fig. a); $\Box = \checkmark \square$ Sketch2 \rightarrow
→ P Hide Sketch (hide Sketch).
Generating of the solid body of the hub
$\Box Extrude \rightarrow \Box = Surface Body (the surface associated with the hub) \rightarrow Details View, Details of Extrude: \Box = \Box = U$
Geometry $\rightarrow \downarrow$ Apply; \Box FD1, Depth (>0) \rightarrow [input the value, 30]; $\downarrow \stackrel{\checkmark}{\rightarrow}$ Generate (generate the solid, fig. b);
Obs. Because in the window that defines extrusion (Details View (Details of Extrude:) in the line Operation
remained, the body of the generated hub is concatenated with the body of the previously generated arm. Tree Outline: $ \downarrow \checkmark \oslash Body \rightarrow Details View, Details of Body; Body \rightarrow [input name, Manivela].$
Generating the radius connection
$\downarrow \bigcirc \text{Blend} \checkmark \rightarrow \downarrow \bigcirc \text{Fixed Radius} \rightarrow \text{Details View, Details of FBlend1: } \Box \square \text{FD1, Radius (>0)} \rightarrow \text{[input the value, 5]; } \Box$
$\sim $ Manivela → \downarrow (edge entity activation) → [it will be selected with \downarrow the edge for connection]; $\downarrow \downarrow$
Geometry $\rightarrow \square$ Apply; $\square \not \not \models$ Generate (generate radius, fig. b)
a. b.
Generating the surface for the shaft
$\textcircled{0}: \Box \text{Concept} \rightarrow \Box \textcircled{2} \text{Surfaces From Sketches} \rightarrow \text{Tree Outline}: \Box \textcircled{1} \textcircled{2} \checkmark XYPlane \rightarrow \Box \checkmark \textcircled{2} \text{Sketch1} \rightarrow \text{Details View},$
Details of SurfaceSk : \exists Base Objects $\rightarrow \exists$ Apply $; \exists$ Generate (generate surface, fig. a); $\exists \neg \neg \square$ Sketch1 \rightarrow
Hide Sketch (hide Sketch).
Generating the solid body of the shaft
$\Box \mathbf{Extrude} \rightarrow \Box \mathbf{\nabla} \mathbf{\nabla} \mathbf{\nabla} \mathbf{\nabla} \mathbf{\nabla} \mathbf{\nabla} \mathbf{\nabla} \mathbf{\nabla}$
Geometry $\rightarrow \downarrow$ Apply; \Box FD1, Depth (>0) \rightarrow [input the value, 50]; $\downarrow \downarrow$ Direction Vector $\rightarrow \downarrow \checkmark {} {} XYPlane$ (normal
plane) $\rightarrow \downarrow$ Apply; $\rightarrow \downarrow$ Operation \rightarrow [select from the list $\rightarrow \checkmark$, \downarrow Add Frozen] (the resulting solid body will be
independent and a separate material will be associated with it); ↓ ³ Generate (generating the solid part, fig. b,
c);
$\downarrow \checkmark \checkmark \lor \lor \downarrow \textcircled{O} \overset{\text{suppless body}}{\longrightarrow} (\text{supress body}).$



C.4. Finite element modelling
C.4.1 Launching the finite element modeling module and set the material characteristics
Launching of the finite element modeling module
\mathbb{N} , Project Schematic : $\square \otimes \mathbb{N}$ Model $\rightarrow \square \otimes \mathbb{C}$ Edit \rightarrow [launch modul <i>Mechanical [ANSYS Multiphysics</i>].
Setting the unit of measure system
$\mathbb{M}_{:}$ Units $\rightarrow \square^{\text{Metric}}$ (mm, kg, N, s, mV, mA) (the system of units of measurement is usually set by default).
Setting the material characteristics
$\begin{array}{ccc} \text{Outline} : & \exists & \forall & \forall$
with $\downarrow \downarrow$, $\downarrow \otimes E335$]; $\downarrow \cong Arbore \rightarrow Details of "Arbore", Material : \downarrow Assignment \rightarrow [select from list with \downarrow \downarrow, \downarrow \otimes C45];$
Disabling redundant entities
Outline: \Box "? \Box Surface Body \rightarrow \Box \Box Suppress Body (deactivation of surface type entities).
Obs. In the specification tree, we observe, as a consequence of the connections between the two bodies, that a
connection Contact Region has been automatically generated in the subdivision \oplus Connections, which
will be further personalized.
C.4.2 Modelling the friction connections
$[M]$, Outline Connections \rightarrow Insert \rightarrow $[M]$ Manual Contact Region \rightarrow
Details of "Bonded - No Selection To No Selection", Definition: $\Box^{Type} \rightarrow [\text{select from list with } \Box^{Frictional}]; \rightarrow \Box$
$\sim $ $\Rightarrow \downarrow $ \square Hide Body (hide the solid Arbore) $\rightarrow \downarrow \square$ \square \rightarrow [with a face of the square profile of the crank
body is selected, fig.a] $\rightarrow \overline{\text{Details of "Frictional - No Selection To No Selection"}}$, Scope . Contact \rightarrow , Apply
(option Contact Bodies is automatically indexed, Manivela); $ \Box $
\longrightarrow Manivela $\rightarrow \square$ Hide Body (hide the solid, Manivela) $\rightarrow \square$ is selected with \square in front of the square
profile of the Arbore body, fig. b] \rightarrow Details of "Frictional - Arbore To Manivela", Scope: \Box Target $\rightarrow \Box$ Apply (option
Target Bodies is automatically indexed, Arbore); \Box Definition: \Box Behavior \rightarrow [select with \Box , \Box Symmetric];
□ Friction Coefficient → [input value, 0.2]; □ Advanced → □ Formulation → [select with □]. □
Augmented Lagrange] (method of solving the nonlinear model).
For each of the other 3 contacts, the sequence will be followed: $\Box = \sqrt{2} Contacts \rightarrow \Box$
Manual Contact Region \rightarrow (continue according to the sequence above, but for another pair of surfaces:,).
After browsing the above sequences in the specification tree $\sqrt{@}$ Contacts it appears
Frictional - Manivela To Arbore for four times.
Obs. For a good convergence of the solution, the entities (surfaces or edges) belonging to the fixed bodies, to
the bodies with increased material rigidity (greater longitudinal elasticity modulus) or smaller curves are
adopted in the window Details of "Frictional at the option.



[the cylindrical surface of the bore in the crank arm shall be selected with \neg] \rightarrow \neg [Apply]; Definition: \neg Define By \rightarrow [select from list \neg]; \neg [components]; \neg [input the value, 15000] (force C).

D. SOLVING THE FEA MODEL

D.1Setting the convergence criterion for solving the nonlinear physical model (with friction)
$\mathbf{M}_{\mathbf{A}}$, Outline : $\mathbf{M}_{\mathbf{A}} \rightarrow \mathbf{M}_{\mathbf{A}}$ Solution (A6) $\mathbf{M}_{\mathbf{A}} \rightarrow \mathbf{M}_{\mathbf{A}}$ Solution Information, Details of "Solution Information",
$\exists \textbf{Solution Information}$: $\exists \textbf{Solution Output} \rightarrow [$ select from list with $\exists \textbf{V}, \exists \textbf{Force Convergence}]$ (the criterion of
force convergence is adopted).
D.2 Setting the results
Setting the total displacement
$\mathbf{M}_{\mathbf{A}}$ Outline $\mathbf{L}_{\mathbf{A}}$ $\mathbf{D}_{\mathbf{A}}$ $\mathbf{D}_{\mathbf{A}$ $\mathbf{D}_{\mathbf{A}}$ $\mathbf{D}_{\mathbf{A}$ $\mathbf{D}_{\mathbf{A}}$ $\mathbf{D}_{\mathbf{A}}$ $\mathbf{D}_{\mathbf{A}}$ $\mathbf{D}_{\mathbf{A}}$ $\mathbf{D}_{\mathbf{A}}$ $\mathbf{D}_{\mathbf{A}}$ $\mathbf{D}_{\mathbf{A}}$ $\mathbf{D}_{\mathbf{A}}$ $\mathbf{D}_{\mathbf{A}$ $\mathbf{D}_{\mathbf{A}}$ $\mathbf{D}_{\mathbf{A}}$ $\mathbf{D}_{\mathbf{A}}$ \mathbf{D}_{A
Setting the equivalent stress
Setting the structural error
Setting parameters from contacts
Setting the design parameters
$ [\%] $ Solution (A6) $ \rightarrow $ $ [] \bigcirc $ Tools $] \rightarrow $ $] \bigcirc $ Stress Tool
L, 🗄 → J Stress Tool J Insert → J Stress Tool → J 🏟 Safety Factor /🏟 Safety Margin / 🍘 Stress Ratio
D.3 Launching the solving module
Outline 🗄

E. POST-PROCESSING OF RESULTS









F. ANALYSIS OF RESULTS

F.1 Interpretation of results

Analyzing the results obtained from modeling and post-processing the results (subchapter E), the following are highlighted:

- As a result of the deformation process of the semi-finished product as a result of the action of the connecting rod (subchapter fig.), Increased displacements (max. 0.4106 mm, subchapter E.1) are observed in the extreme area of the crank.
- The equivalent stress has increased values (max 705.62 MPa; subchapter E.2, fig. A, b, c) in the areas of the connecting rod, in the corner of the square profile of the crank and in the area of connection of the arm to the hub.
- In the subcap. E.4 the states of the contacts are visualized (subchapter E.5, fig. A) and the values of some contact parameters: surface tension tangential friction max. 54,563 MPa, fig. b; pressure max 457.04 MPa, fig. c; relative slip max 0.039 mm, fig. d; the game (jump) max 1.91 mm, fig. e; penetration max 0.00477 mm, fig. f. These values are useful for designing the shaft-hub assembly (eg starting from the maximum pressure value determines the hardness of the active contact surfaces).
- Highlighting the field of the safety factor related to the allowable values (subchapter) is particularly useful in designing to identify the areas with values of this unacceptable factor; thus, dimensional and shape corrections can be made to obtain the optimal structure (subchapter F.2).

F.2 Analysis of the precision and convergence of solving the nonlinear model

Following the analysis of the obtained results, related to precision and convergence, as a result, of the modeling and AEF (subcap. E.3 and E.6) the following are highlighted:

- The maximum structural error in the connection areas of the square profile of the connecting rod has a reduced value (0.23538 mJ corresponding to the areas with increased values of the equivalent stress) shows an accuracy of the acceptable results (stresss).
- The convergence of the model solution is done quickly in 6 steps (subchapter E.6) and the calculation time is reduced.

F.3 Design studies

In order to avoid the occurrence of the rupture micro-cracks in the connection areas of the square profile, a fact highlighted by increased values of the equivalent stress (subchapter E.2) but also by subunit values of the safety factor (subchapter E.6) are imposed, on on the one hand, *dimensional changes* (eg, increase of the radius of connection of the square profile; increase of the radius of the bore in the arm; increase of the radius of connection of the arm to the hub and / or increase of the thickness of the arm or, on the other hand, *changes of the shape*.

In case of dimensional changes, it is necessary to modify the analysis model and to solve the model by going through the successions: M, Tree Outline: change the dimension value \swarrow Generate; M, Outline: \Box M, Outline: \Box M, (M), $(\textcircled{$

and reinterpreted. If after the stage of dimensional changes the crank structure is not optimal (minimum weight and equivalent stresses, respectively, safety factors in permissible fields), the shape of the model is changed (eg adopting an assembly after a hexagonal profile and / or modification of the arm shape by the insertion of a bump and / or a rib).



G. CONCLUSIONS

The modeling and analysis with finite elements of this paper were also done with didactic purpose following the initiation of the user with the main stages of development of an application of FEA in ANSYS Workbench, which insists, in particular, on the modeling and analysis of a deformable element and of its contacts with another adjacent element.

The adopted FEA model involves considering the multiple surface-to-surface friction contacts of a square / hexagonal joint between two elements of linear behavior. The loads are introduced distributed on a cylindrical surface and considering the existence of the bearing.

As a result of solving the model with finite elements nonlinearly adopting the method of force convergence, results have been obtained with increased precision, the values of the obtained parameters (displacements, stresses, safety factors) being useful for designing the crank element considering the profiled assembly with square profile.